

Dr Oliver Mathematics
GCSE Mathematics
2024 June Paper 3H: Calculator
1 hour 30 minutes

The total number of marks available is 80.

You must write down all the stages in your working.

1. Find the highest common factor (HCF) of 63 and 105. (2)

2. (a) (i) Write (1)

$$5.3 \times 10^4$$

as an ordinary number.

(ii) Write (1)

$$7.4 \times 10^{-5}$$

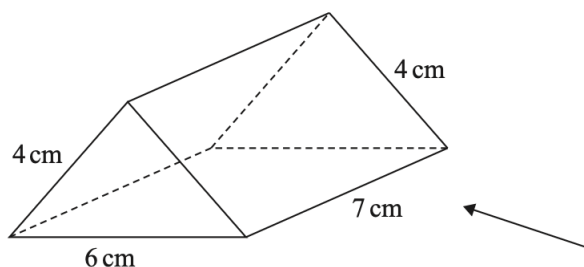
as an ordinary number.

(b) Calculate the value of (2)

$$9.7 \times 10^6 + 2.45 \times 10^7.$$

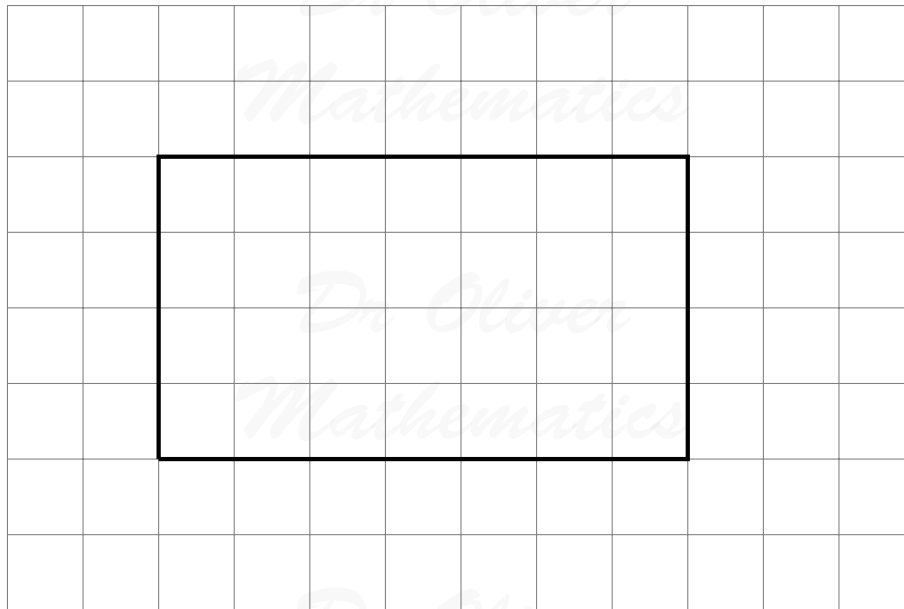
Give your answer in standard form.

3. The diagram shows a solid triangular prism.



Rana is trying to draw the side elevation of the solid prism from the direction of the arrow.

Here is her answer on a centimetre grid.



- (a) Explain why Rana's side elevation is not correct. (1)
- (b) On the centimetre grid below, draw a plan of the solid prism. (2)



4. A company has 25 000 workers. (4)
- The number of workers increases at a rate of 6% per year for 3 years.
- Calculate the total number of workers at the end of the 3 years.

5. Habib has two identical tins. (4)

He puts 600 grams of flour into one of the tins.

The flour fills the tin completely.

The density of the flour is 0.6 g/cm^3 .

Habib puts 600 grams of salt into the other tin.

The salt does **not** fill the tin completely.

The volume of the space in the tin that is **not** filled with salt is 700 cm^3 .

Work out the density of the salt.

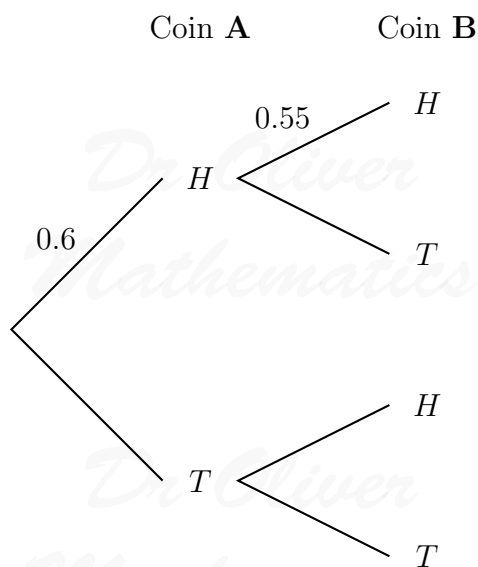
You must show all your working.

6. Tim has two biased coins, coin **A** and coin **B**.

He is going to throw both coins.

- The probability that coin **A** will land on heads is 0.6.
- The probability that coin **B** will land on heads is 0.55.

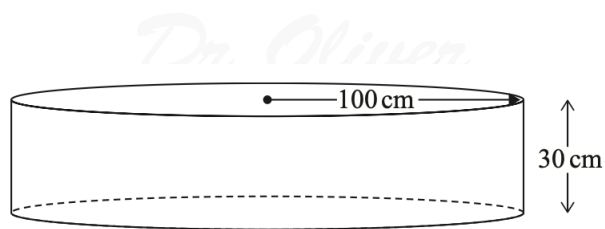
- (a) Complete the probability tree diagram.



Tim throws coin **A** once and he throws coin **B** once.

- (b) Work out the probability that both coins land on heads. (2)

7. A paddling pool is in the shape of a cylinder. (4)



- The pool has radius 100 cm.
- The pool has depth 30 cm.
- The pool is empty.
- It is then filled with water at a rate of 250 cm^3 per second.

Work out the number of minutes it takes to fill the pool completely.

Give your answer correct to the nearest minute.

You must show all your working.

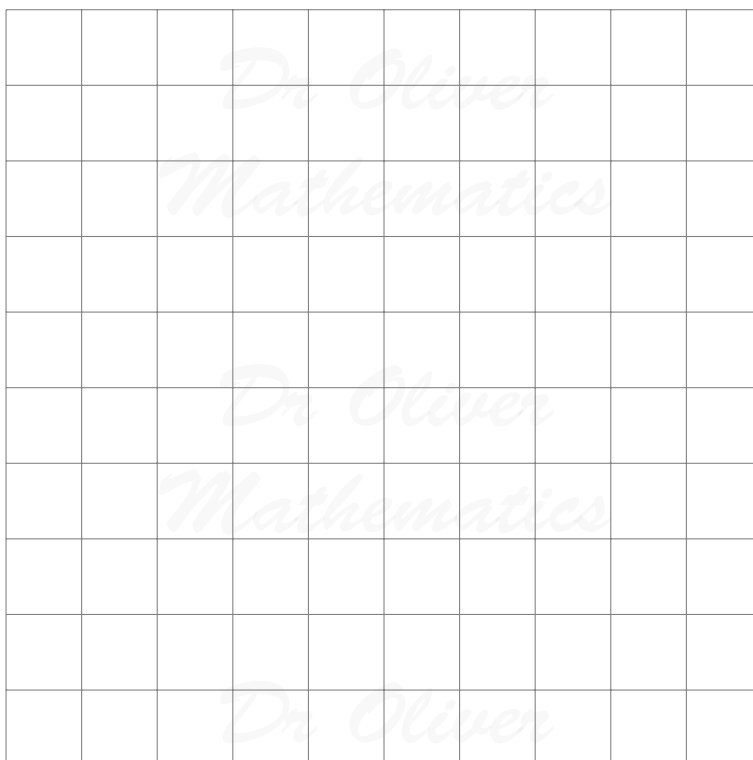
8.

(3)

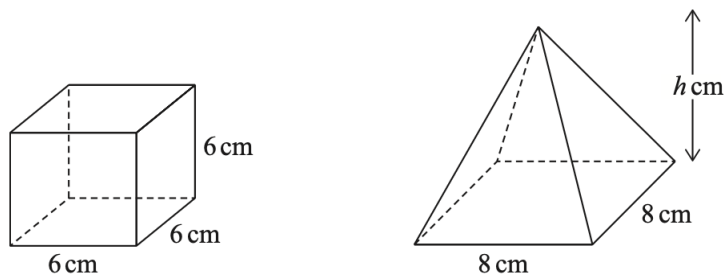
$$\mathbf{a} = \begin{pmatrix} 3 \\ 2 \end{pmatrix} \text{ and } \mathbf{b} = \begin{pmatrix} -1 \\ 4 \end{pmatrix}.$$

On the grid below, draw and label the vector

$$2\mathbf{a} + \mathbf{b}.$$



9. The diagram shows a cube and a square-based pyramid. (3)



The volume of the cube is equal to the volume of the pyramid.

Work out the perpendicular height, h cm, of the pyramid.

10. There are only red counters and yellow counters in bag A . (3)

Number of red counters : number of yellow counters = 3 : 5.

There are only green counters and blue counters in bag B .

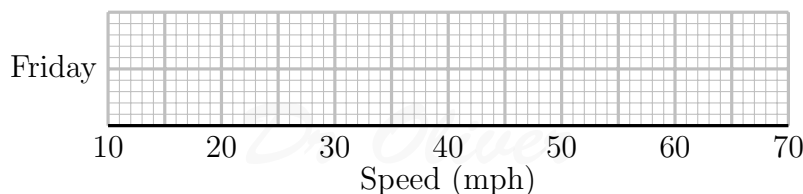
The number of counters in bag B is half the number of counters in bag A .

Given that there are x red counters in bag A , use algebra to show that the total number of counters in bag A and bag B is $4x$.

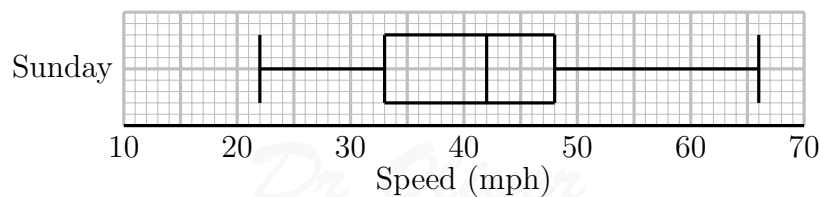
11. Mina records the speeds, in mph, of some cars on a road on Friday.
She uses her results to work out the information in this table.

	Speed (mph)
Lowest speed	25
Lower quartile	35
Median	40
Interquartile range	12
Range	37

- (a) On the grid, draw a box plot to show the information in the table. (3)

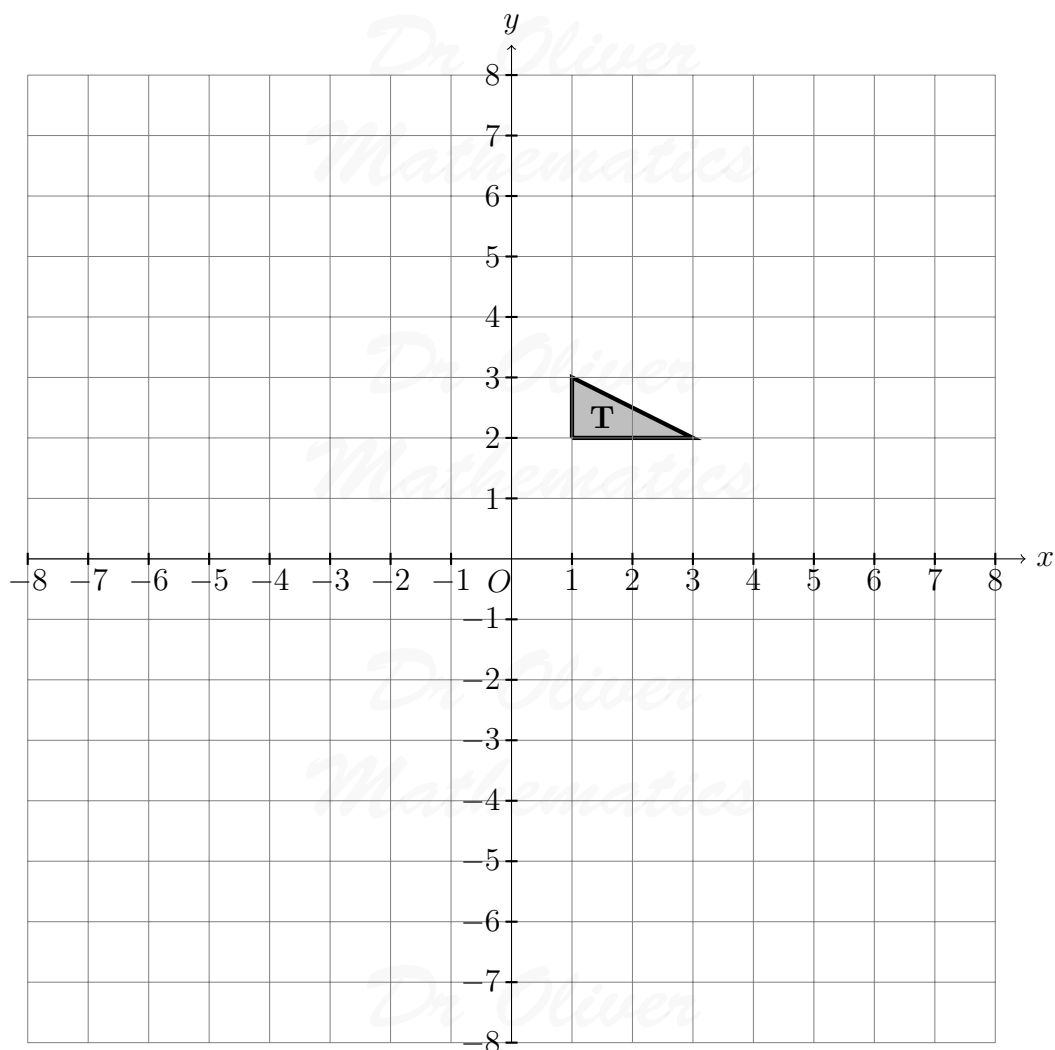


Mina also records the speeds of some cars on the same road on Sunday.



- (b) Compare the distribution of the speeds on Friday with the distribution of the speeds on Sunday. (2)

12. The diagram shows triangle **T** drawn on a grid. (2)



Enlarge triangle **T** by scale factor -2 , with centre of enlargement $(0, 0)$.

13. There are 30 students in a class. (2)
A teacher is going to choose at random 2 of the students.

Work out the number of different pairs of students that the teacher can choose.

14. At the start of 2022 Kim invested some money in a savings account. (4)
The account paid 3.5% compound interest each year.

At the end of 2022, interest was added to the account then Kim took £750 from the account.

At the end of 2023, interest was added to the account then Kim took £1 000 from the account.

There was then £2937.14 in the account.

Work out how much money Kim invested at the start of 2022.
You must show all your working.

15. (a) Simplify fully (1)

$$\frac{(a-3)^2}{5(a-3)}.$$

- (b) Factorise (2)

$$3k^2 + 11k - 4.$$

- (c) Simplify fully (3)

$$\frac{4-x^2}{x^2+3x} \div \frac{x+2}{x+3}.$$

16. The functions f and g are given by

$$f(x) = \frac{12}{x+1} \text{ and } g(x) = 5 - 3x.$$

- (a) Find (1)

$$f(-3).$$

- (b) Find (2)

$$f g(1).$$

- (c) Find (2)

$$g^{-1}(4).$$

17. A ball is thrown upwards and reaches a maximum height. (3)
The ball then falls and bounces repeatedly.

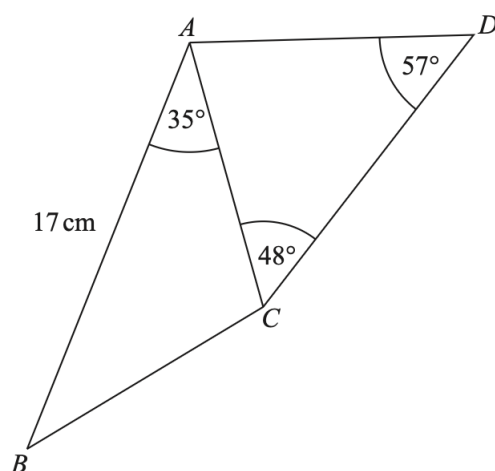
- After the n th bounce, the ball reaches a height of h_n .
- After the next bounce, the ball reaches a height given by

$$h_{n+1} = 0.55 h_n.$$

- After the 1st bounce, the ball reaches a height of 8 metres.

What height does the ball reach after the 4th bounce?

18. $ABCD$ is a quadrilateral. (5)



The area of triangle ABC is 54 cm^2 .

Calculate the area of triangle ACD .

Give your answer correct to 3 significant figures.

19. (3)

$$R = \frac{P}{Q}.$$

- $P = 5.88 \times 10^8$, correct to 3 significant figures.
- $Q = 3.6 \times 10^5$, correct to 2 significant figures.

Work out the lower bound for R .

Give your answer as an ordinary number correct to the nearest integer.

You must show all your working.

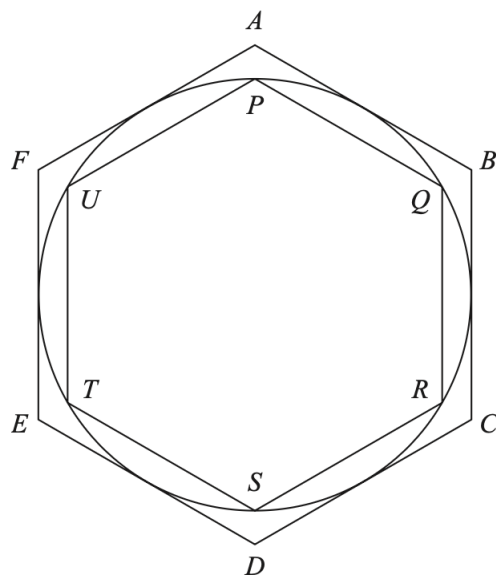
20. $(x - 4)$, $(x + 2)$, and $(3x + 1)$ are three consecutive terms of an arithmetic sequence.

(a) Find the value of x . (2)

$(y - 4)$, $(y + 2)$, and $(3y + 1)$ are three consecutive terms of an geometric sequence.

(b) Find the possible values of y . (5)

21. The diagram shows a circle, radius r cm and two regular hexagons. (4)



- Each side of the larger hexagon $ABCDEF$ is a tangent to the circle.
- Each side of the smaller hexagon $PQRSTU$ is a chord of the circle.

By considering perimeters, show that

$$3 < \pi < 2\sqrt{3}.$$