# Dr Oliver Mathematics Mathematics: National Qualifications N5 2023 Paper 2: Calculator <br> 1 hour 30 minutes 

The total number of marks available is 50 .
You must write down all the stages in your working.

1. A caravan was bought for $£ 20000$.

It depreciated by $11 \%$ in the first year.
It then depreciated by a further $6 \%$ each year over the next two years.

Calculate the value of the caravan three years after it was bought.
2. The mass of a helium atom is $6.64 \times 10^{-24}$ grams.

A flask contains 300 grams of helium.
Calculate the number of helium atoms in this flask.

Give your answer in scientific notation, correct to 3 significant figures.
3. The diagram shows part of a football pitch.


The penalty spot is marked at point $C$.
$A B$ is an arc of a circle, centre $C$, radius 9.15 metres.

Calculate the length of the arc $A B$.
4. The diagram shows triangle $J K L$.

- Angle $K J L=25^{\circ}$.
- $J L=10$ metres.
- $K L=7$ metres.




Calculate the size of angle $J K L$.
5. A logo consists of an H-shape and a regular decagon.

The diagram represents the logo.


Calculate the size of the shaded angle.
6. Nadim bought a flat last year.

The value of the flat has increased by $8 \%$ and it is now worth $£ 94500$.

Calculate how much Nadim paid for the flat.
7. Change the subject of the formula

$$
P=\frac{1}{3} m n-r
$$

to $m$.
8. A wooden beam is used to support a wall built on horizontal ground as shown in the diagram.


- The edge of the beam, $A B$, is 8 metres long.
- $C$ is at the foot of the wall.
- $A$ is 7 metres from $C$.
- $B$ is 4 metres from $C$.

Determine whether the wall is perpendicular to the ground.
Justify your answer.
9. A concrete block is in the shape of a large pyramid with a small pyramid removed.


The large pyramid has a square base of length 90 centimetres.
The small pyramid has a square base of length 40 centimetres and a height of 48 centimetres.

The block has height 60 centimetres.
Calculate the volume of the block.
10. Express

$$
\frac{7}{x-3}-\frac{2}{x}, x \neq 3, x \neq 0
$$

as a single fraction in its simplest form.
11. Anna has a grandfather clock in her house.


The height of the tip of the hour hand above the floor, in centimetres, is given by

$$
h=20 \cos x^{\circ}+147,
$$

where $x^{\circ}$ is the angle the hour hand has rotated through since 12 o'clock.


Calculate the first two values of $x$ for which the tip of the hour hand is 150 centimetres above the floor.
12. Simplify

$$
\begin{equation*}
\frac{x^{2}-16}{x^{2}+x-20} . \tag{3}
\end{equation*}
$$

13. Simplify

$$
\begin{equation*}
2 \sin ^{2} x^{\circ}+2 \cos ^{2} x^{\circ} . \tag{2}
\end{equation*}
$$

## Show your working.

14. A storage unit, built in the shape of a cuboid, is shown.


It has length $(x+7)$ metres, breadth $x$ metres, and height 2 metres. The volume of this unit is 45 cubic metres.
(a) Show that

$$
\begin{equation*}
2 x^{2}+14 x-45=0 \tag{2}
\end{equation*}
$$

Give your answer correct to 1 decimal place.
15. In the diagram:

- $A C$ is perpendicular to $B C$,
- $A B=18$ centimetres,
- $B D=6$ centimetres, and
- $B C=8$ centimetres.


The area of triangle $A D E$ is 160 square centimetres.

Calculate the length of $A E$.

