# Dr Oliver Mathematics GCSE Mathematics 2020 November Paper 2H: Calculator 1 hour 30 minutes 

The total number of marks available is 80 .
You must write down all the stages in your working.

1. The scatter graph shows information about the amount of rainfall, in mm, and the number of hours of sunshine for each of ten English towns on the same day.

Number of hours of sunshine


One of the points is an outlier.
(a) Write down the coordinates of this point.
(b) Ignoring the outlier, describe the relationship between the amount of rainfall and the number of hours of sunshine.

On the same day in another English town there were 7 hours of sunshine.
(c) Using the scatter graph, estimate the amount of rainfall in this town on this day.
2. The front elevation and the plan of a solid are shown on the grid.

On the grid, draw the side elevation of the solid from the direction of the arrow.

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3. Here are the first five terms of an arithmetic sequence:

$$
\begin{array}{lllll}
7 & 13 & 19 & 25 & 31 .
\end{array}
$$

(a) Find an expression, in terms of $n$, for the $n$th term of this sequence.

The $n$th term of a different sequence is

$$
8-6 n .
$$

(b) Is -58 a term of this sequence?

You must show how you get your answer.
4. The diagram shows a plan of Jason's garden.

- $A B C O$ and $D E F O$ are rectangles,
- $C D O$ is a right-angled triangle,
- $A F O$ is a sector of a circle with centre $O$, and
- angle $A O F=90^{\circ}$.


Jason is going to cover his garden with grass seed.

- Each bag of grass seed covers $14 \mathrm{~m}^{2}$ of garden.
- Each bag of grass seed costs $£ 10.95$.

Work out how much it will cost Jason to buy all the bags of grass seed he needs.
5. Work out the value of $x$.


Give your answer correct to 3 significant figures.
6. Ella invests $£ 7000$ for 2 years in an account paying compound interest.

- In the first year, the rate of interest is $3 \%$.
- In the second year, the rate of interest is $1.5 \%$.

Work out the value of Ella's investment at the end of 2 years.
7. Here is the graph of

$$
y=x^{2}-6 x+4
$$


(a) Write down the $y$-intercept of the graph of

$$
\begin{equation*}
y=x^{2}-6 x+4 \tag{1}
\end{equation*}
$$

(b) Write down the coordinates of the turning point of the graph of

$$
\begin{equation*}
y=x^{2}-6 x+4 \tag{1}
\end{equation*}
$$

(c) Use the graph to find estimates for the roots of

$$
\begin{equation*}
x^{2}-6 x+4=0 \tag{2}
\end{equation*}
$$

8. Chanda buys a necklace for $£ 120$.

She sells the necklace for $£ 135$.
Work out her percentage profit.
9. Here are the equations of two straight lines:

$$
\begin{equation*}
y=\frac{1}{2} x-6 \text { and } 6 y=3 x+7 \tag{2}
\end{equation*}
$$

Oscar says that these lines are parallel.

Is Oscar correct?
You must give a reason for your answer.
10. Aaliyah bought a car.

- In the first year after she bought the car, its value depreciated at a rate of $23 \%$ per annum.
- In the second year after she bought the car, its value depreciated at a rate of $19 \%$ per annum.

At the end of the second year the car was worth $£ 10$ 914.75.
What was the value of the car when Aaliyah bought it?
11. In an experiment, 60 students each completed a puzzle.

The cumulative frequency graph shows information about the times taken for the 60 students to complete the puzzle.



For these 60 students,

- the least time taken was 24 seconds and
- the greatest time taken was 96 seconds.

On the grid below, draw a box plot for the distribution of the times taken by the students.

12. The number of insects in a population at the start of the Year $n$ is $P_{n}$.

The number of insects in the population at the start of Year $(n+1)$ is $P_{n+1}$ where

$$
P_{n+1}=k P_{n} .
$$

Given that $k$ has a constant value of 1.13,
(a) find out how many years it takes for the number of insects in the population to double.
You must show how you get your answer.
The value of $k$ actually increases year on year from its value of 1.13 in Year 1.
(b) How does this affect your answer to part (a)?
13. $A$ and $B$ are points on a centimetre grid.
$A$ is the point with coordinates $(-7,6)$.
$B$ is the point with coordinates $(8,5)$.
Work out the length of $A B$.
Give your answer correct to 1 decimal place.
14. Using algebra, prove that $1.06 \dot{2}$ can be written as $1 \frac{14}{225}$.
15. Faiza is studying the population of rabbits in a park.

She wants to estimate the number of rabbits in the park.

On Monday she catches a random sample of 20 rabbits in the park, marks each rabbit with a tag and releases them back into the park.

On Tuesday she catches a random sample of 42 rabbits in the park. 12 of the rabbits are marked with a tag.
(a) Find an estimate for the number of rabbits in the park.

Albie is studying the population of rabbits in a wood.
One day, he catches 55 rabbits and finds that 40 of these rabbits are marked with a tag.
Albie estimates there are 50 rabbits in the wood.
(b) Explain why Albie's estimate cannot be correct.
16. The shaded region shown on the grid is bounded by four straight lines.


Find the four inequalities that define the shaded region.
17. The diagram shows two similar solid triangular prisms, $\mathbf{A}$ and $\mathbf{B}$.


The volume of prism $\mathbf{A}$ is $58.806 \mathrm{~cm}^{3}$.
The volume of prism B is $1587.762 \mathrm{~cm}^{3}$.
The cross section of each prism is a right-angled triangle.
For prism B,

- the length of the base of the triangle is 8.1 cm and
- the area of the triangle is $43.74 \mathrm{~cm}^{2}$.

The height of the triangle for prism $\mathbf{A}$ is $h \mathrm{~cm}$.
Work out the value of $h$.
18. Here is a triangle


Work out the area of the triangle.
Give your answer correct to 3 significant figures.
19. Solve

$$
\begin{equation*}
6 x^{2}+5 x-6=0 . \tag{3}
\end{equation*}
$$

20. $A B C D E F G H$ is a cuboid.


- $A D=9 \mathrm{~cm}$.
- $F D=13 \mathrm{~cm}$.
- Angle $G H F=49^{\circ}$.

Work out the size of angle $F A H$.
Give your answer correct to the nearest degree.
21. The graph below gives the volume, in litres, of water in a container $t$ seconds after the water starts to fill the container.
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(a) Calculate an estimate for the gradient of the graph when $t=17.5$.

You must show how you get your answer.
(b) Describe fully what the gradient in part (a) represents.
22. $\mathrm{f}(x)=\sqrt[3]{x}$.
$\mathrm{g}(x)=2 x+3$.
$\mathrm{h}(x)=\mathrm{fg}(x)$.
Find $\mathrm{h}^{-1}(x)$.
23. A race is measured to have a distance of 10.6 km , correct to the nearest 0.1 km .

Sam runs the race in a time of 31 minutes 48 seconds, correct to the nearest second.
Sam's average speed in this race is $V \mathrm{~km} /$ hour.
By considering bounds, calculate the value of $V$ to a suitable degree of accuracy. You must show all your working and give a reason for your answer.
24. A circle has equation

$$
\begin{equation*}
x^{2}+y^{2}=12.25 \tag{4}
\end{equation*}
$$

The point $P$ lies on the circle.
The coordinates of $P$ are (2.1, 2.8).
The line $\mathbf{L}$ is the tangent to the circle at point P .
Find an equation of $\mathbf{L}$.
Give your answer in the form

$$
a x+b y=c,
$$

where $a, b$, and $c$ are integers.

