

**Dr Oliver Mathematics**  
**AQA GCSE Mathematics**  
**2018 November Paper 2: Calculator**  
**1 hour 30 minutes**

The total number of marks available is 80.

You must write down all the stages in your working.

1. What does  $(A \cap B)$  represent in  $P(A \cap B)$ ? (1)

Circle your answer.

$A$  or  $B$  or both    $A$  but not  $B$    not  $A$  and not  $B$     $A$  and  $B$

2.  $P$  is  $(4, 9)$  and  $Q$  is  $(-2, 1)$ . (1)

Circle the midpoint of  $PQ$ .

$(1, 5)$     $(3, 4)$     $(3, 5)$     $(6, 8)$

3. Which of these is a geometric progression? (1)

Circle your answer.

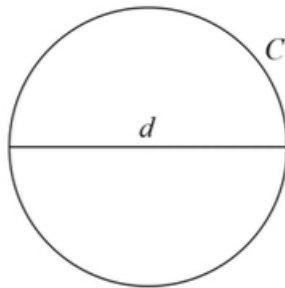
1, 3, 5, 7, 9   1, 3, 6, 10, 15   1, 4, 9, 16, 25   1, 3, 9, 27, 81

4. The bearing of  $A$  from  $B$  is  $310^\circ$ . (1)

Circle the bearing of  $B$  from  $A$ .

$050^\circ$     $110^\circ$     $130^\circ$     $220^\circ$

5. A circle has circumference  $C$  and diameter  $d$ . (1)



$$C = kd.$$

What value does the constant  $k$  represent?

6. Here is some information about 20 trains leaving a station.

Number of minutes late, $t$	Number of trains	Midpoint
$0 \leq t < 5$	12	
$5 \leq t < 10$	7	
$10 \leq t < 15$	1	
$t \geq 15$	0	

(a) Work out an estimate of the mean number of minutes late. (3)

The station manager looks at the information in more detail.

Number of minutes late, $t$	Number of trains
$0 \leq t < 2$	12
$2 \leq t < 4$	0
$4 \leq t < 6$	7
$6 \leq t < 8$	0
$8 \leq t < 10$	0
$10 \leq t < 12$	1

He works out an estimate of the mean using this information.

(b) How does his estimate compare with the answer to part (a)? (1)  
Tick **one** box.

Higher than part (a)

Same as part (a)

Lower than part (a)

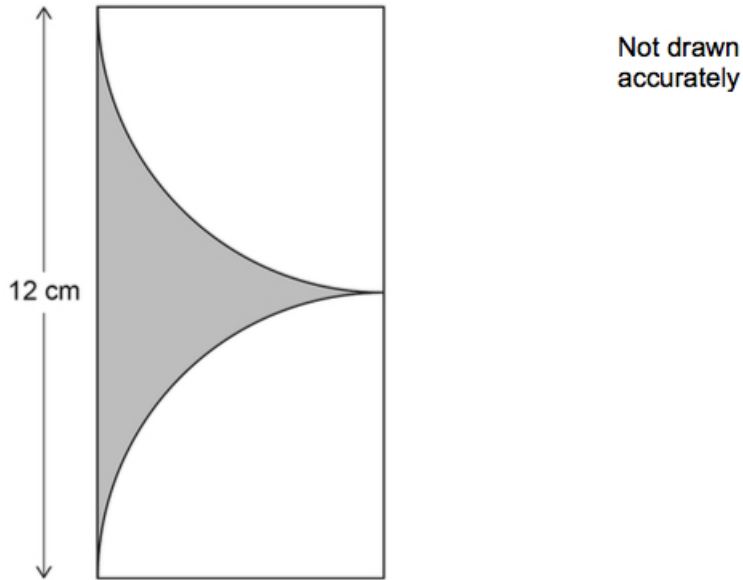
Not possible to tell

7. Work out the values of  $a$  and  $b$  in the identity (4)

$$5(7x + 8) + 3(2x + b) \equiv ax + 13.$$

8. Two identical quarter circles are cut from a rectangle as shown.

(4)



Work out the shaded area.

9. The diagrams show the position of a tap when off and fully on. The tap is fully on when the angle of turn is  $180^\circ$ .

(4)

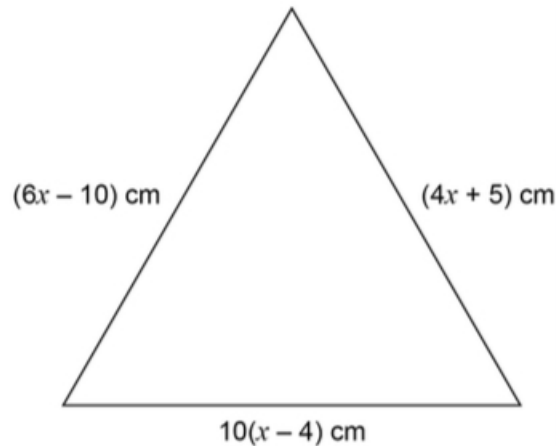


When fully on, water flows out of the tap at 14 litres per minute. The rate at which water flows out is in direct proportion to the angle of turn. The tap is turned  $135^\circ$ .



The water flows into a tank with a capacity of 79.8 litres.  
Will it take **less than**  $7\frac{1}{2}$  minutes to fill the tank?  
You **must** show your working.

10. This triangle is equilateral. (5)



Not drawn accurately

Is the perimeter of the triangle greater than one metre?  
You **must** show your working.

11. An approximation for the value of  $\pi$  is given by (2)

$$4 \left( 1 - \frac{22}{57} + \frac{22}{85} - \frac{22}{105} + \frac{22}{117} - \frac{22}{242} \right).$$

Use your calculator to show that this approximation is within 0.1 of 3.14.

12. Work out (2)

$$\frac{9.12 \times 10^{10}}{3.2 \times 10^4}.$$

Give your answer in standard form.

13. Ashraf is going to put boxes into a crate. (2)

- The crate is a cuboid measuring 2.5 m by 2 m by 1.2 m.
- Each box is a cube of length 50 cm.

He does these calculations.

volume of crate	=	$2.5 \times 2 \times 1.2$
	=	$6 \text{ m}^3$
volume of one box	=	$0.5 \times 0.5 \times 0.5$
	=	$0.125 \text{ m}^3$
number of boxes	=	$6 \div 0.125$
	=	$48$

He claims, "I can put 48 boxes in the crate."

Evaluate Ashraf's method **and** claim.

14. The cross section of a prism has  $n$  sides. (1)

Circle the expression for the number of edges of the prism.

$$2n \quad 3n \quad n + 2 \quad 2n + 3$$

15. The volume of a medal is  $45 \text{ cm}^3$ . (4)

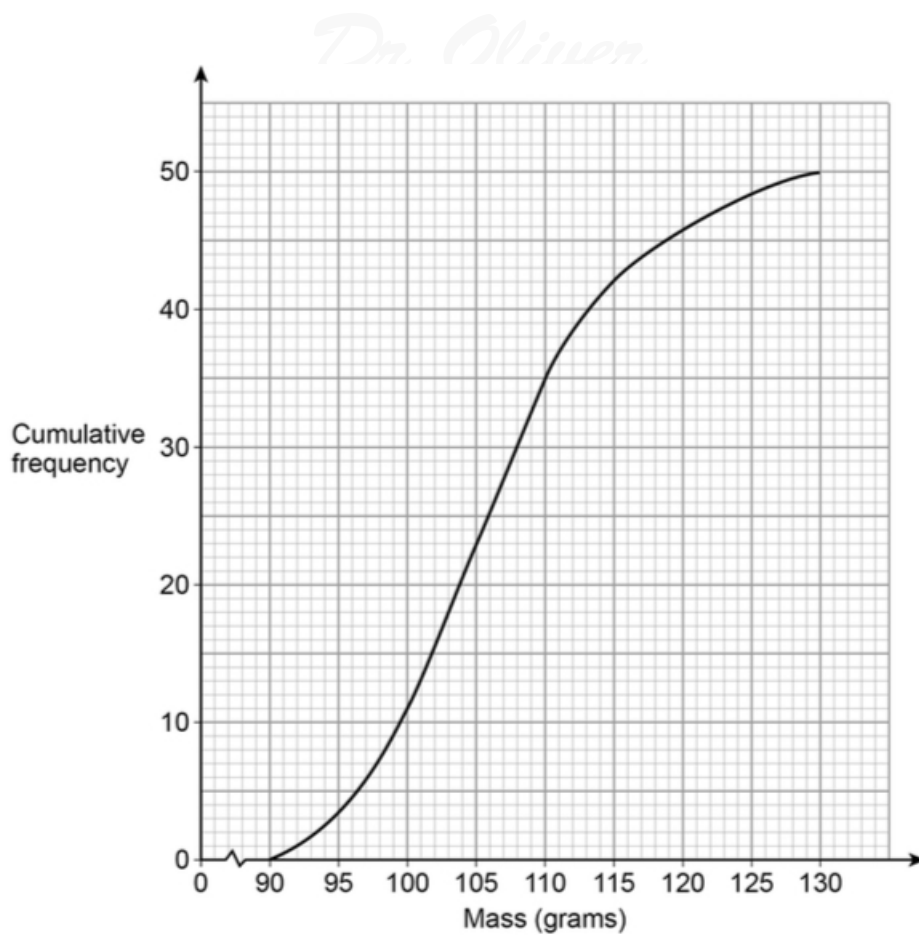
The medal is made from copper and tin.

volume of copper : volume of tin = 22 : 3
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- The density of copper is  $8.96 \text{ g/cm}^3$ .
- The density of tin is  $7.31 \text{ g/cm}^3$

Work out the mass of the medal.

16. The cumulative frequency graph shows information about the masses of 50 apples.



(a) Use the graph to estimate the median mass of the apples. (1)

(b) Estimate the proportion of the apples that have a mass greater than 115 grams. (2)

17.  $a$  is a prime number. (1)

$b$  is an even number.

$$N = a^2 + ab.$$

Circle the correct statement about  $N$ .

could be even or odd    always even    always prime    always odd

18. A bag contains 20 discs.

10 are red, 7 are blue, and 3 are green.

Marnie takes a disc at random before putting it back in the bag.

Nick then takes a disc at random before putting it back in the bag.

Olly then takes a disc at random.

- (a) Work out the probability that they all take a red disc. (2)

All 20 discs are in the bag.

- Reggie takes three discs at random, one after the other.
- After he takes a disc he does **not** put it back in the bag.

Reggie's first disc is blue.

- (b) Work out the probability that all three discs are different colours. (3)

19. There are four starters and ten main courses to choose from. (3)

Two of the starters and three of the main courses are suitable for vegans.

<p style="text-align: center;"><b>Lunch</b></p> <p style="text-align: center;">Choose one starter and one main course</p>
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What percentage of the possible lunches have **both** courses suitable for vegans?

20.  $n$  is a positive integer. (3)

Prove algebraically that

$$2n^2 \left( \frac{3}{n} + n \right) + 6n(n^2 - 1)$$

is a cube number.

21.  $y$  is inversely proportional to  $\sqrt{x}$ .

$y = 4$  when  $x = 9$ .

- (a) Work out an equation connecting  $y$  and  $x$ . (3)

- (b) Work out the value of  $y$  when  $x = 25$ . (2)

22. Simplify fully (3)

$$\frac{x^5 - 4x^3}{3x - 6}$$

23.  $PQR$  is a straight line. (1)

$PQ : QR = 3 : 1$ .

$\frac{PQ}{QR} = a$ .

Not drawn  
accurately



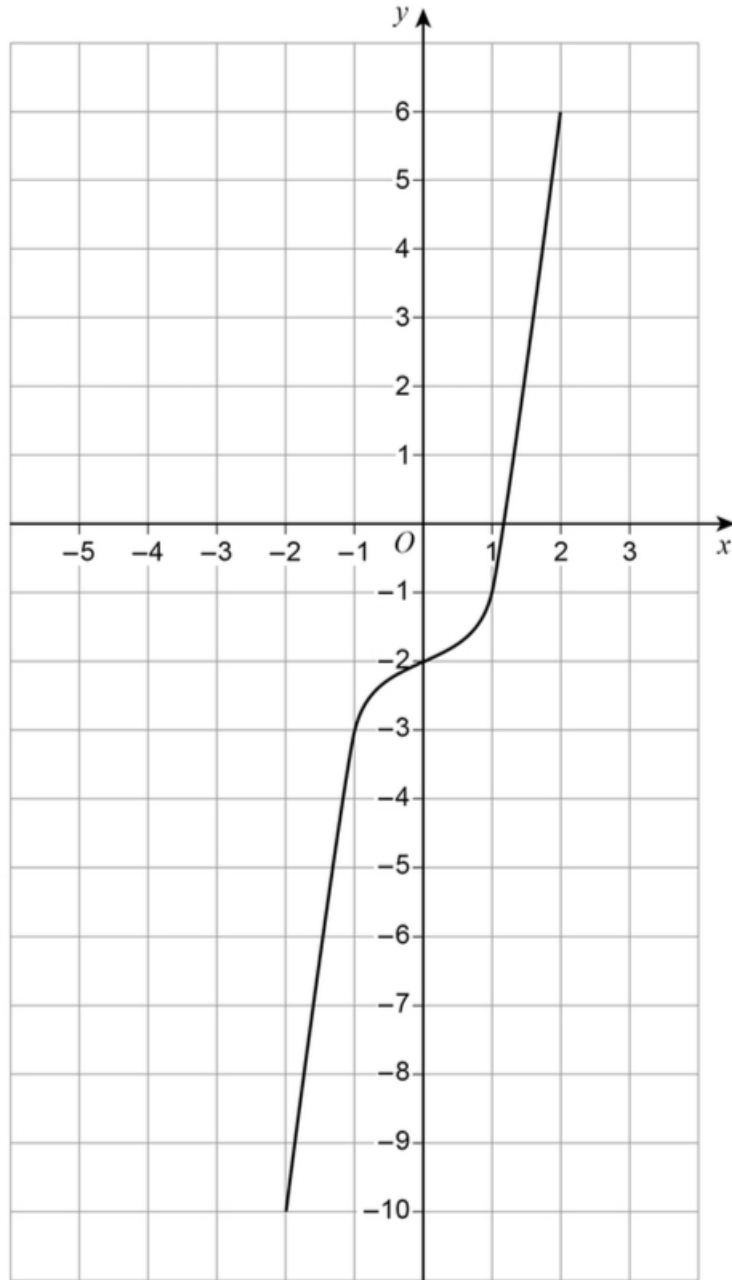
Circle the vector  $\overrightarrow{RQ}$ .

$\frac{1}{3}\mathbf{a}$     $\frac{1}{4}\mathbf{a}$     $-\frac{1}{3}\mathbf{a}$     $-\frac{1}{4}\mathbf{a}$

24. Here is a sketch of  $y = f(x)$ .

The curve passes through the points  $(-2, -10)$ ,  $(-1, -3)$ ,  $(0, -2)$ ,  $(1, -1)$ , and  $(2, 6)$ .

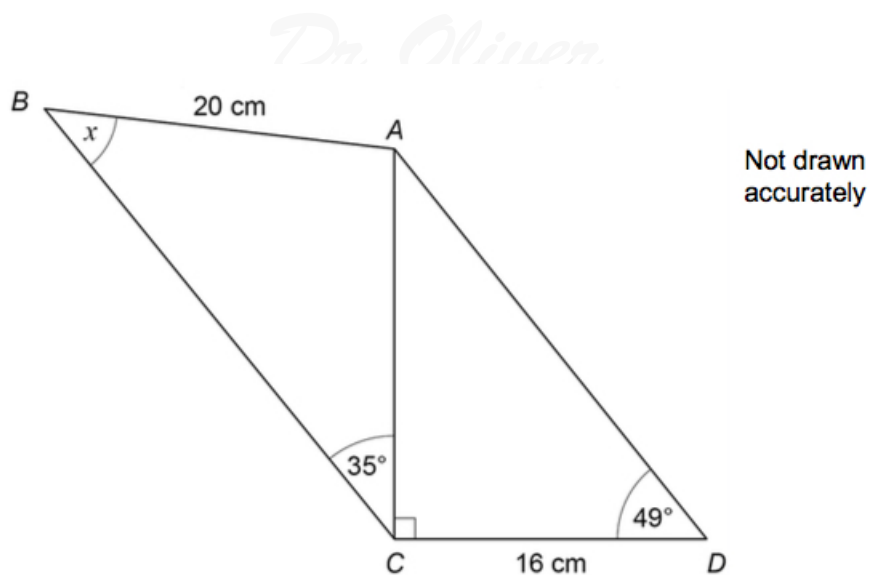
(2)



On the grid, sketch the curve  $y = f(x + 2)$ .

25.  $ABC$  and  $ACD$  are triangles.

(5)



Work out the size of angle  $x$ .

26.

$$f(x) = \frac{x}{x+2} \text{ and } g(x) = x^2 - 2.$$

Work out  $f \circ g(x)$ .

Give your answer in the form

$$a + bx^n,$$

where  $a$ ,  $b$ , and  $n$  are integers.

27. The point  $(3, \frac{1}{64})$  lies on the curve  $y = k^x$ , where  $k$  is a constant.

Show that the point  $(\frac{1}{2}, \frac{1}{2})$  lies on the curve.

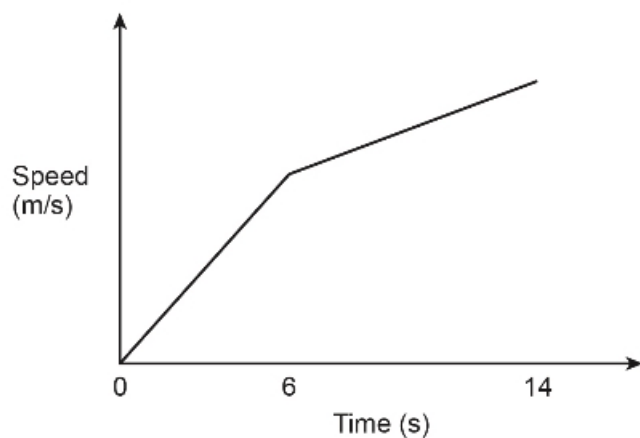
28. Izzy runs an 80-metre race in 14 seconds.

- During the first 6 seconds her speed increases at a constant rate.
- During the last 8 seconds her speed increases at a different constant rate.
- Her speed at 14 seconds is 2 m/s more than her speed at 6 seconds.

Here is a sketch of her speed-time graph.

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Not drawn accurately

- (a) Work out her acceleration during the last 8 seconds. (2)  
State the units of your answer.

When Izzy finishes the 80-metre race, her speed is  $v$  m/s.

- (b) Work out the value of  $v$ . (4)

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