Dr Oliver Mathematics Worked Examples Area 3

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1. In Figure 2, a small circle is drawn inside a larger circle. The small circle crosses the centre of the large circle, as shown.

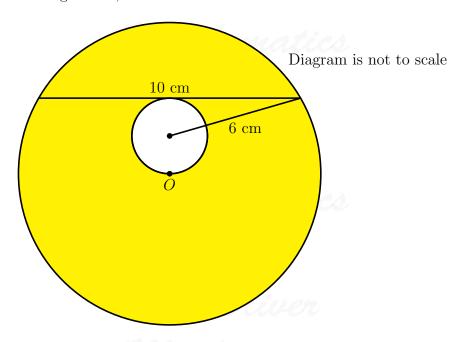


Figure 1: two circles

The length of the horizontal chord of the bigger half-circle is tangent to the smaller half-circle is 10 cm.

Moreover, the length of this line, which connects the centre of the small circle to the right-hand end of the chord, is 6 cm.

Find the shaded area in yellow.

Solution

Let r cm be the radius of the smaller circle and let R cm be the radius of the larger circle:



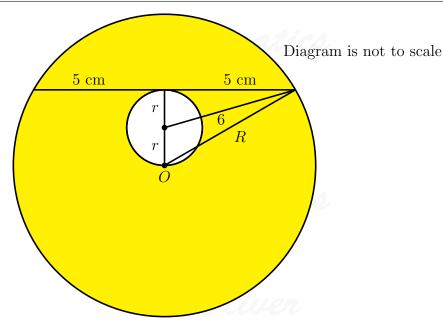


Figure 2: two circles

Two lots of Pythagoras' theorem:

$$r^2 + 5^2 = 6^2 \Rightarrow r^2 + 25 = 36$$
$$\Rightarrow r^2 = 11$$

and

$$(2r)^2 + 5^2 = R^2 \Rightarrow 4r^2 + 25 = R^2$$
$$\Rightarrow 4(11) + 25 = R^2$$
$$\Rightarrow 44 + 25 = R^2$$
$$\Rightarrow R^2 = 69;$$

hence,

shaded area =
$$(\pi \times 69) - (\pi \times 11)$$

= $\pi(69 - 11)$
= $\underline{58\pi \text{ cm}^2}$.