## Dr Oliver Mathematics Worked Examples Find the Area of the Yellow Region 1

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1. In Figure 1, a circle, centred at O and of radius 17 cm, parallel chords AB and CD are drawn.

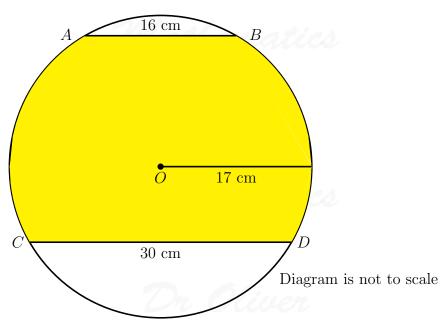


Figure 1: a circle, centred at O and of radius 17 cm

These parallel chords are, respectively, AB = 16 cm and CD = 30 cm.

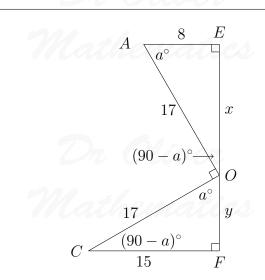
Find the area which is coloured in yellow.

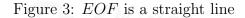
## Solution

Let E be the midpoint on AB and let F be the midpoint on CD so that EOF is a straight line.

Let OE = x cm and OF = y cm, as shown in Figure 2:

$$\frac{4}{17} + \frac{5}{17} + \frac{5}{17}$$





$$\angle AOE + \angle AOC + \angle COF = 180 \Rightarrow (90 - a) + \angle AOC + a = 180$$
$$\Rightarrow \angle AOC = 90^{\circ};$$

exactly the same goes for  $\angle BOD$ :

 $\angle BOD = 90^{\circ}.$ 

(In fact,

$$\angle AOD = \tan^{-1} \frac{8}{15} = 28.072\,486\,94^{\circ} \text{ (FCD)}$$

and

$$\angle COE = \tan^{-1} \frac{15}{8} = 61.92751306^{\circ} \text{ (FCD)};$$

the reader will not be surprised to find the sum the angles equals  $90^{\circ}$ .)

Now,

$$\operatorname{area}_{\triangle OAB} = \frac{1}{2} \times 16 \times 15$$
$$= 120 \text{ cm}^2$$

and

$$\operatorname{area}_{\triangle OCD} = \frac{1}{2} \times 30 \times 8$$
$$= 120 \text{ cm}^2.$$

Next,

area<sub>sector OAC</sub> = 
$$\frac{1}{4} \times (\pi \times 17^2)$$
  
=  $\frac{289}{4}\pi$ 

and

area<sub>sector OBD</sub> = 
$$\frac{1}{4} \times (\pi \times 17^2)$$
  
=  $\frac{289}{4}\pi$ .

Finally,

area = 
$$120 + 120 + \frac{289}{4}\pi + \frac{289}{4}\pi$$
  
=  $(240 + \frac{289}{2}\pi)$  cm<sup>2</sup>.

## Mathematics





