

**Dr Oliver Mathematics**  
**GCSE Mathematics**  
**2006 June Paper 5H: Non-Calculator**  
**2 hours**

The total number of marks available is 100.

You must write down all the stages in your working.

1.  $3x^2 = 108$ .

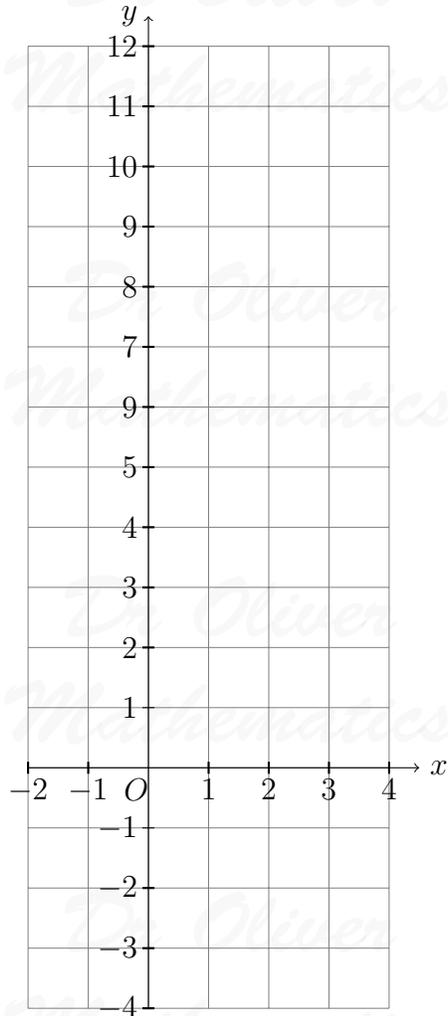
(a) Find the value of  $x$ . (2)

(b) Express 108 as a product of its prime factors. (3)

2. (a) Complete the table of values for  $y = x^2 - 3x + 1$ . (2)

|     |    |    |   |    |   |   |   |
|-----|----|----|---|----|---|---|---|
| $x$ | -2 | -1 | 0 | 1  | 2 | 3 | 4 |
| $y$ | 11 |    | 1 | -1 |   |   | 5 |

(b) On the grid, draw the graph of  $y = x^2 - 3x + 1$ . (2)



- (c) Use your graph to estimate the values of  $x$  for which  $y = 3$ . (2)
3. A silver chain has a volume of  $5 \text{ cm}^3$ . (2)  
The density of silver is  $10.5 \text{ grams per cm}^3$ .  
Work out the mass of the silver chain.
4.  $ABCD$  is a rectangle. (4)



Shade the set of points inside the rectangle which are **both** more than 4 centimetres from the point  $A$  **and** more than 1 centimetre from the line  $DC$ .

5. Fred did a survey of the time, in seconds, people spent in a queue at a supermarket. Information about the times is shown in the table. (2)

| Time ( $t$ seconds) | Frequency |
|---------------------|-----------|
| $0 < t \leq 40$     | 8         |
| $40 < t \leq 80$    | 12        |
| $80 < t \leq 120$   | 14        |
| $120 < t \leq 160$  | 16        |
| $160 < t \leq 200$  | 10        |

A person is selected at random from the people in Fred's survey. Work out an estimate for the probability that the person selected spent more than 120 seconds in the queue.

6. Work out an estimate for (3)

$$\frac{412 \times 5.904}{0.195}$$

7. A gold necklace has a mass of 127 grams, correct to the nearest gram.
- (a) Write down the **least** possible mass of the necklace. (1)
- (b) Write down the **greatest** possible mass of the necklace. (1)
8. A student wanted to find out how many pizzas adults ate. He used this question on a questionnaire. (2)

How many pizzas have you eaten?

A few

A lot

This is not a good question.

Design a better question that the student can use to find out how many pizzas adults ate.

You should include some response boxes.

9. Write in standard form

(a) 456 000,

(1)

(b) 0.000 34,

(1)

(c)  $16 \times 10^7$ .

(1)

10. (a) Factorise

(2)

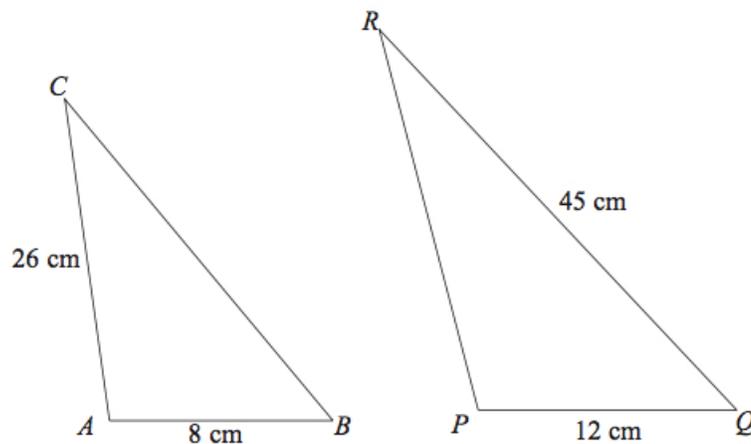
$$x^2 + 6x + 8.$$

(b) Solve

(1)

$$x^2 + 6x + 8 = 0.$$

11. The two triangles  $ABC$  and  $PQR$  are mathematically similar.



Diagrams **NOT**  
accurately drawn

Angle  $A =$  angle  $P$ .

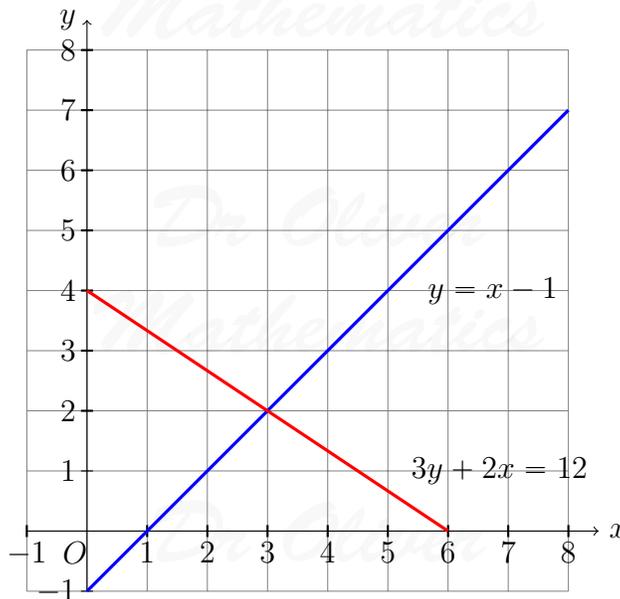
Angle  $B =$  angle  $Q$ .

$AB = 8$  cm.

$AC = 26$  cm.  
 $PQ = 12$  cm.  
 $QR = 45$  cm.

- (a) Work out the length of  $PR$ . (2)
- (b) Work out the length of  $BC$ . (2)

12. The graphs of the straight lines with equations  $3y + 2x = 12$  and  $y = x - 1$  have been drawn on the grid.



- (a) Use the graphs to solve the simultaneous equations (1)

$$\begin{aligned}
 3y + 2x &= 12 \\
 y &= x - 1.
 \end{aligned}$$

- (b)  $3y + 2x > 12$ . (3)
- $y < x - 1$ .
- $x < 6$ .
- $x$  and  $y$  are integers.

On the grid, mark with a cross ( $\checkmark$ ) each of the four points which satisfies all these 3 inequalities.

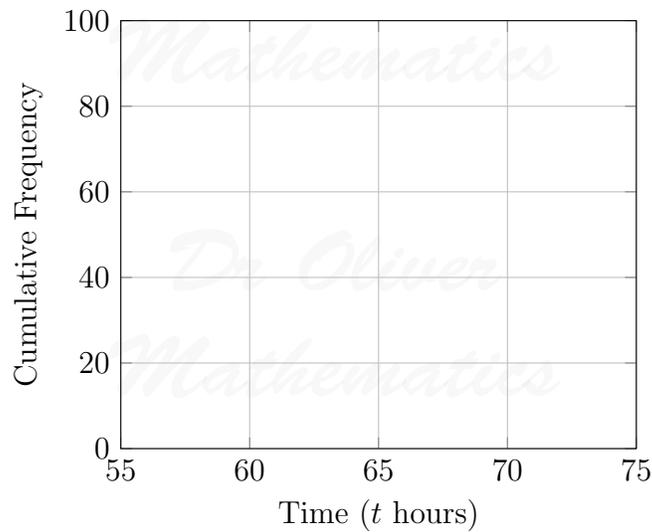
13. Hajra's weekly pay this year is £240.  
 This is 20% more than her weekly pay last year.  
 Bill says, "This means Hajra's weekly pay last year was £192."  
 Bill is wrong.

- (a) Explain why. (1)
- (b) Workout Hajra's weekly pay last year. (2)

14. A company tested 100 batteries.  
The table shows information about the number of hours that the batteries lasted.

| Time ( $t$ hours) | Frequency |
|-------------------|-----------|
| $50 < t \leq 55$  | 12        |
| $55 < t \leq 60$  | 21        |
| $60 < t \leq 65$  | 36        |
| $65 < t \leq 70$  | 23        |
| $70 < t \leq 75$  | 8         |

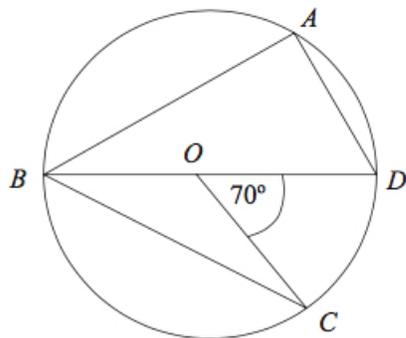
- (a) Complete the cumulative frequency table for this information. (1)
- (b) On the grid, draw a cumulative frequency graph for your completed table. (2)



- (c) Use your completed graph to find an estimate for the median time.  
You must state the units of your answer. (2)

15.  $A$ ,  $B$ ,  $C$ , and  $D$  are points on the circumference of a circle, centre  $O$ .

Diagram NOT accurately drawn



$BOD$  is a straight line.

Angle  $COD = 70^\circ$ .

- (a) Find the size of angle  $BAD$ . (2)  
Give a reason for your answer.
- (b) Find the size of angle  $CBD$ . (2)  
Give a reason for your answer.

16. The time,  $T$  seconds, it takes a water heater to boil some water is directly proportional to the mass of water,  $m$  kg, in the water heater.  
When  $m = 250$ ,  $T = 600$ .

- (a) Find  $T$  when  $m = 400$ . (3)

The time,  $T$  seconds, it takes a water heater to boil a constant mass of water is inversely proportional to the power,  $P$  watts, of the water heater.  
When  $P = 1400$ ,  $T = 360$ .

- (b) Find the value of  $T$  when  $P = 900$ . (3)

17. The diagram is a sketch.

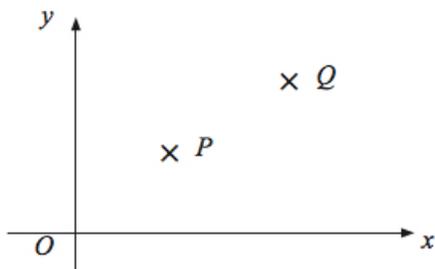


Diagram NOT accurately drawn

$P$  is the point  $(2, 3)$ .

$Q$  is the point  $(6, 6)$ .

- (a) Write down the vector  $\overrightarrow{PQ}$ . (2)

Write your answer as a column vector  $\begin{pmatrix} x \\ y \end{pmatrix}$ .

$PQRS$  is a parallelogram.

$$\overrightarrow{PR} = \begin{pmatrix} 4 \\ 7 \end{pmatrix}.$$

- (b) Find the vector  $\overrightarrow{QS}$ . (2)

Write your answer as a column vector  $\begin{pmatrix} x \\ y \end{pmatrix}$ .

18. (a) Solve (2)

$$\frac{3}{x} + \frac{3}{2x} = 2.$$

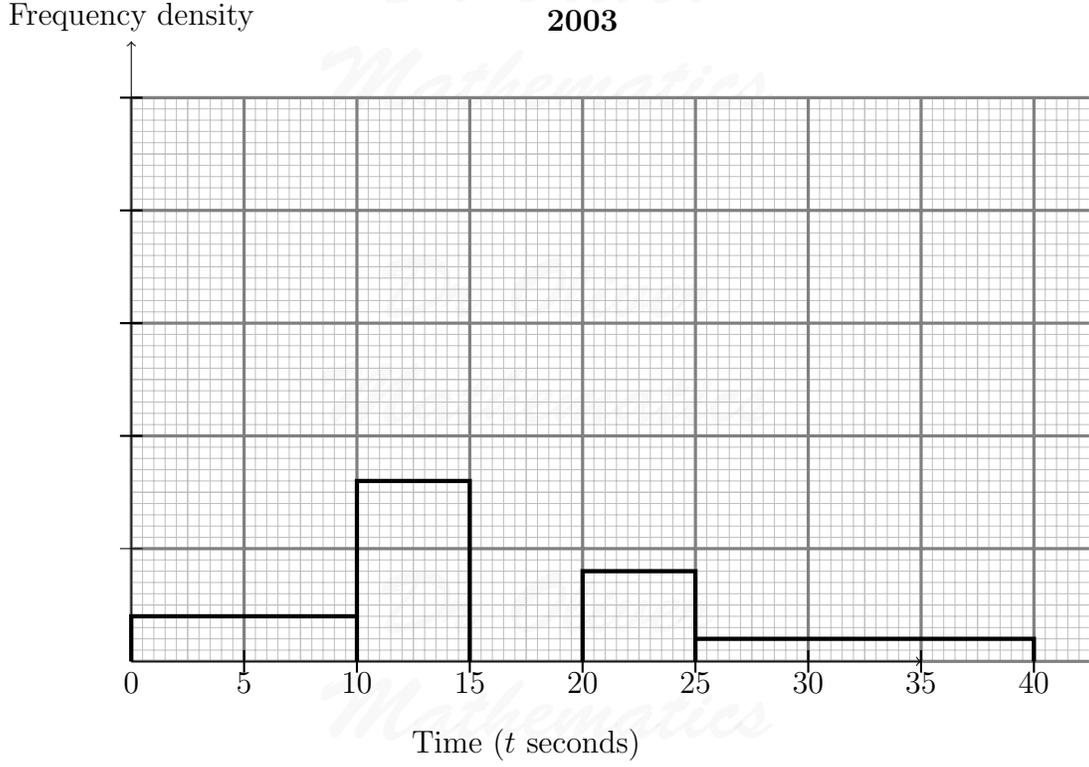
- (b) Using your answer to part (a), or otherwise, solve (3)

$$\frac{3}{(y-1)^2} + \frac{3}{2(y-1)^2} = 2.$$

19. The table and histogram show information about the length of time it took 165 adults to connect to the internet.

| Time ( $t$ seconds) | Frequency |
|---------------------|-----------|
| $0 < t \leq 10$     | 20        |
| $10 < t \leq 15$    |           |
| $15 < t \leq 17.5$  | 30        |
| $17.5 < t \leq 20$  | 40        |
| $20 < t \leq 25$    |           |
| $25 < t \leq 40$    |           |

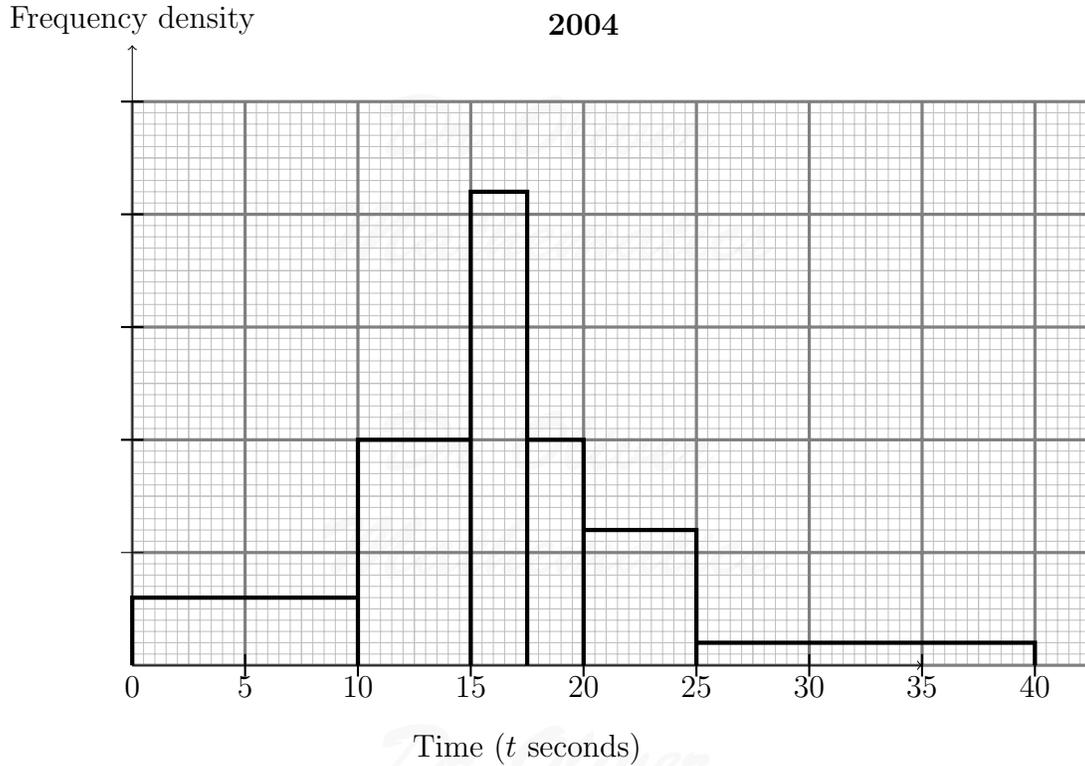
None of the adults took more than 40 seconds to connect to the internet.



(a) Use the table to complete the histogram. (2)

(b) Use the histogram to complete the table. (2)

The histogram shows information about the time it took some children to connect to the internet.



None of the children took more than 40 seconds to connect to the internet.

110 children took up to 12.5 seconds to connect to the internet.

- (c) Work out an estimate for the number of children who took 21 seconds or more to connect to the internet. (3)

20. (a) Write down the value of  $8^{\frac{1}{3}}$ . (1)

$8\sqrt{8}$  can be written in the form  $8^k$ .

- (b) Find the value of  $k$ . (1)

$8\sqrt{8}$  can also be expressed in the form  $m\sqrt{2}$  where  $m$  is a positive integer.

- (c) Express  $8\sqrt{8}$  in the form  $m\sqrt{2}$ . (2)

- (d) Rationalise the denominator of  $\frac{1}{8\sqrt{8}}$ . (2)

Give your answer in the form  $\frac{\sqrt{2}}{p}$  where  $p$  is a positive integer.

21.  $ABCD$  is a square.

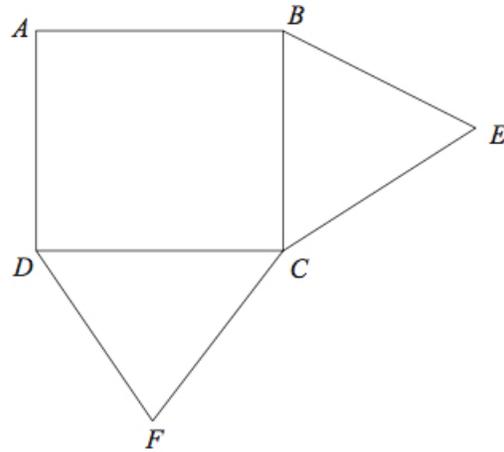


Diagram NOT accurately drawn

$BEC$  and  $DCF$  are equilateral triangles.

(a) Prove that triangle  $ECD$  is congruent to triangle  $BCF$ . (3)

$G$  is the point such that  $BEGF$  is a parallelogram.

(b) Prove that  $ED = EG$ . (2)

22. (4)

$$P = \frac{n^2 + a}{n + a}$$

Rearrange the formula to make  $a$  the subject.

23. (a) Factorise (2)

$$2x^2 - 7x + 6.$$

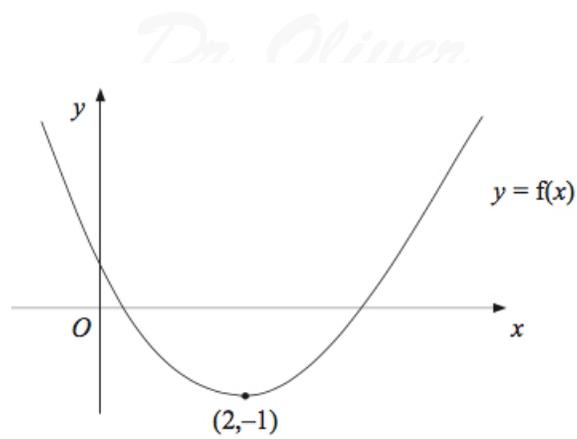
(b) (i) Factorise fully (4)

$$(n^2 - a^2) - (n - a)^2.$$

$n$  and  $a$  are integers.

(ii) Explain why  $(n^2 - a^2) - (n - a)^2$  is always an even integer.

24. The diagram shows part of the curve with equation  $y = f(x)$ .



The minimum point of the curve is at  $(2, -1)$ .

- (a) Write down the coordinates of the minimum point of the curve with equation (3)
- (i)  $y = f(x + 2)$ ,
  - (ii)  $y = 3f(x)$ ,
  - (iii)  $y = f(2x)$ .

The curve  $y = f(x)$  is reflected in the  $y$ -axis.

- (b) Find the equation of the curve following this transformation. (1)

The curve with equation  $y = f(x)$  has been transformed to give the curve with equation  $y = f(x) + 2$ .

- (c) Describe the transformation. (1)